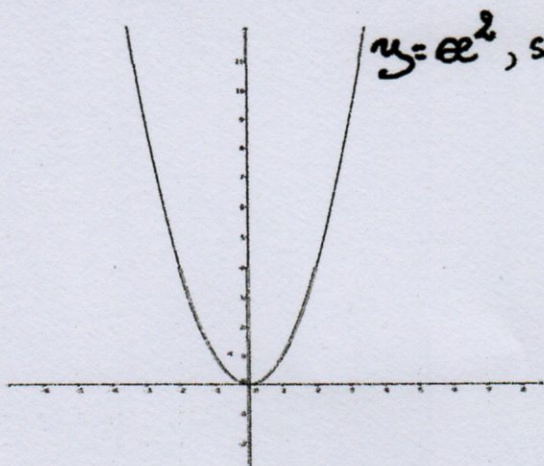


TS

### Limites de fonctions numériques à une variable



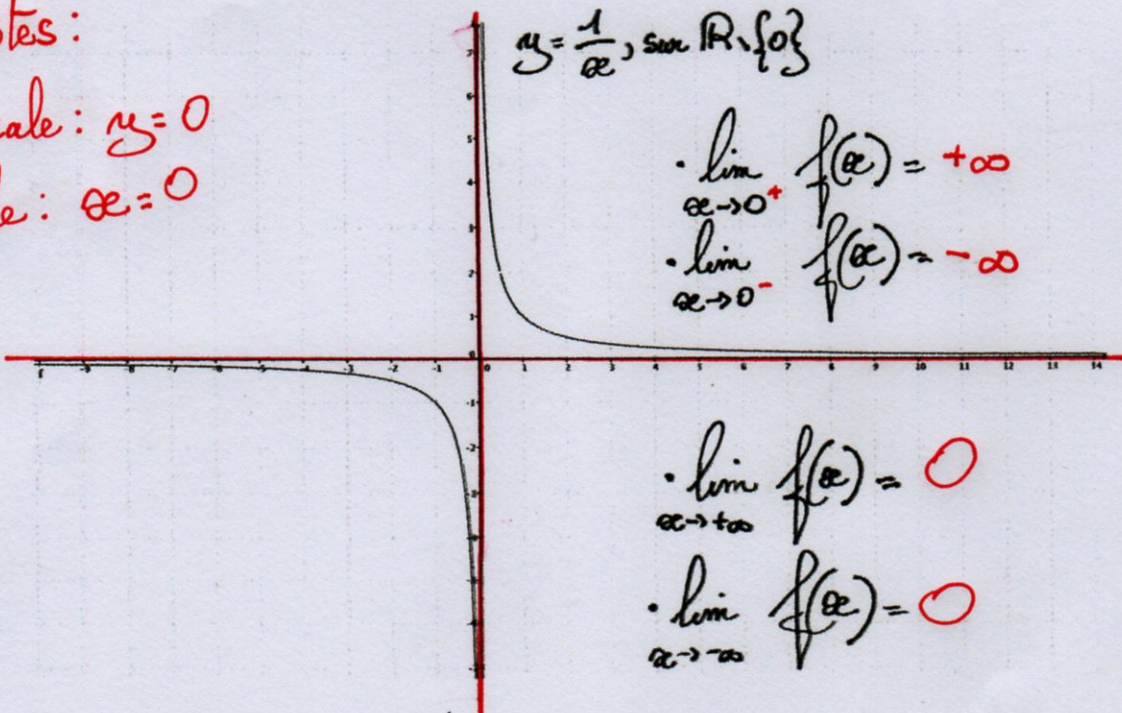
$$y = x^2, \text{ sur } \mathbb{R}$$

- $\lim_{x \rightarrow 0} f(x) = f(0) = 0$
- $\lim_{x \rightarrow +\infty} f(x) = +\infty$
- $\lim_{x \rightarrow -\infty} f(x) = +\infty$

Asymptotes:

- horizontale:  $y = 0$
- verticale:  $x = 0$

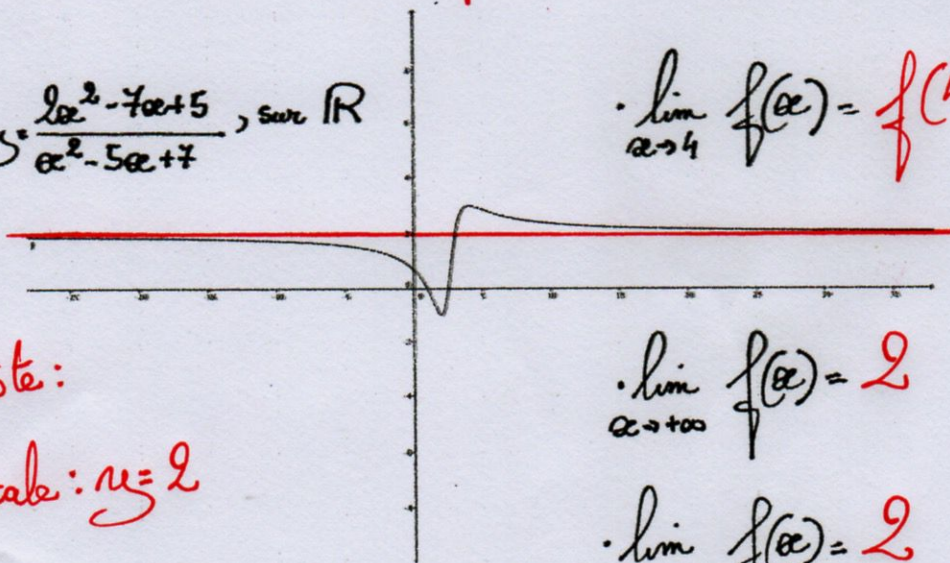
$$y = \frac{1}{x}, \text{ sur } \mathbb{R} \setminus \{0\}$$



- $\lim_{x \rightarrow 0^+} f(x) = +\infty$
- $\lim_{x \rightarrow 0^-} f(x) = -\infty$

- $\lim_{x \rightarrow +\infty} f(x) = 0$
- $\lim_{x \rightarrow -\infty} f(x) = 0$

$$y = \frac{2x^2 - 7x + 5}{x^2 - 5x + 7}, \text{ sur } \mathbb{R}$$



- $\lim_{x \rightarrow 4} f(x) = f(4) = 3$

Asymptote:

- horizontale:  $y = 2$

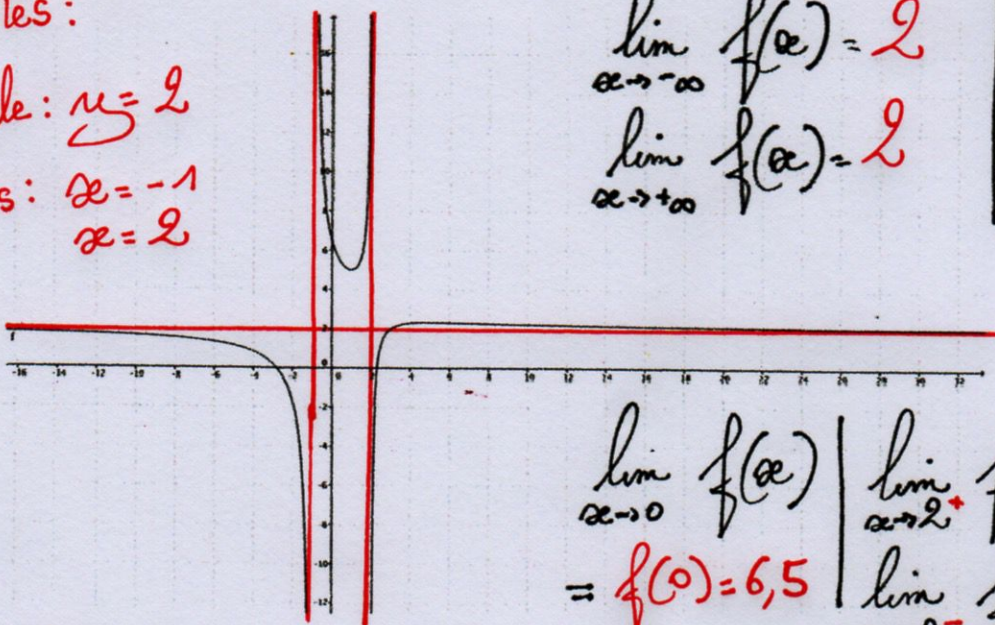
- $\lim_{x \rightarrow +\infty} f(x) = 2$
- $\lim_{x \rightarrow -\infty} f(x) = 2$

TS

$$y = \frac{2x^2 + x - 13}{x^2 - x - 2} \text{ sur } \mathbb{R} \setminus \{-1; 2\}$$

Asymptotes:

- horizontales:  $y = 2$
- verticales:  $x = -1$   
 $x = 2$



$$\lim_{x \rightarrow -\infty} f(x) = 2$$

$$\lim_{x \rightarrow +\infty} f(x) = 2$$

$$\lim_{x \rightarrow -1^-} f(x) = -\infty$$

$$\lim_{x \rightarrow -1^+} f(x) = +\infty$$

$$\lim_{x \rightarrow 0} f(x) = f(0) = 6,5$$

$$\lim_{x \rightarrow -\infty} f(x) = +\infty$$

$$\lim_{x \rightarrow +\infty} f(x) = -\infty$$

$$\lim_{x \rightarrow 2^+} f(x) = +\infty$$

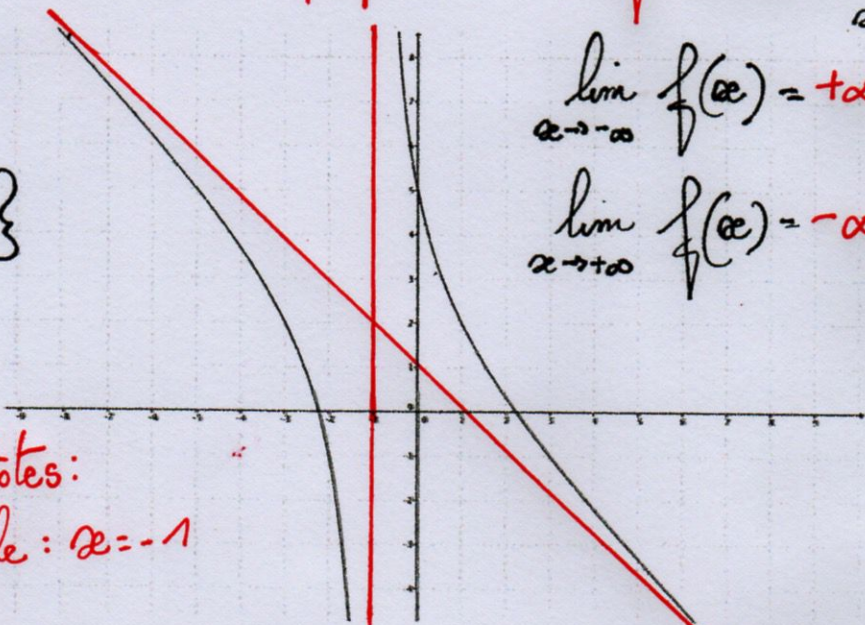
$$\lim_{x \rightarrow 2^-} f(x) = -\infty$$

$$\lim_{x \rightarrow -1^-} f(x) = -\infty$$

$$\lim_{x \rightarrow -1^+} f(x) = +\infty$$

$$y = \frac{-x^2 + 5}{x - 1}$$

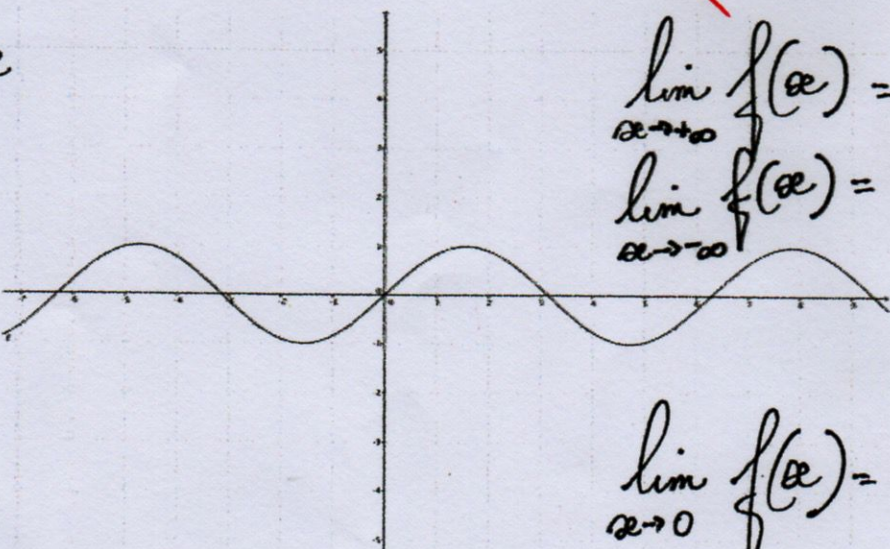
sur  $\mathbb{R} \setminus \{1\}$



Asymptotes:

- verticale:  $x = 1$
- oblique!

$$y = \sin x \text{ sur } \mathbb{R}$$



$\left. \begin{array}{l} \lim_{x \rightarrow +\infty} f(x) = ? \\ \lim_{x \rightarrow -\infty} f(x) = ? \end{array} \right\}$  n'existent pas!

$$\lim_{x \rightarrow 0} f(x) = 0$$